

**Exercise 1**

Give the formal definition of the Vigenère cipher and show that with a key as long as the plaintext, picked at random it is a perfect cipher.

**Exercise 2**

A flawed RSA setup initializes the cipher with  $n = 2p$ , where  $p$  is a large prime ( $> 1024$  bits). Describe an attack that computes the private exponent  $a$  from  $n$  and the public exponent  $b$ . Illustrate using small numbers.

**Exercise 3**

It is proposed a payment system for a drink machine in which the machine and the payment device (for example a RFID key) share a cryptographic key  $k$  and the recharge is done as follows:

1. The user inserts the payment device and the coins in the machine;
2. The machine counts the amount of money  $M$  inserted and sends message  $E_k(M)$  to the payment device.  $M$  is padded with zeros as needed to reach the block size;
3. The device decrypts the message and increases the credit of the amount  $M$ .

Show an attack and discuss possible fixes to the system.

**Exercise 4**

In order to protect 8-bytes long system passwords, they are hashed using the following function:

$$h(\text{pwd}, \text{salt}) = \text{pwd} \oplus \text{salt}$$

The 8-bytes long `salt` is randomly picked for each user and, as usual, is stored in the password file together with the hash of the password. To verify a password the system follows the standard procedure: looks into the file, reads the user `salt` and recompute the hash of the password and the salt. The result is compared with the one stored in the file.

Describe an attack that permits to compute a valid password from the password file. Explain what is the vulnerability and what would be a possible fix.

**Exercise 5 (optional, gives extra score)**

Explain in detail the Meet-in-the-middle attacks for iterated ciphers.